

Nuclear spin effects in semiconductor quantum dots

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The interaction of an electronic spin with its nuclear environment, an issue known as the central spin problem, has been the subject of considerable attention due to its relevance for spin-based quantum computation using semiconductor quantum dots. Independent control of the nuclear spin bath using nuclear magnetic resonance techniques and dynamic nuclear polarization using the central spin itself offer unique possibilities for manipulating the nuclear bath with significant consequences for the coherence and controlled manipulation of the central spin. Here we review some of the recent optical and transport experiments that have explored this central spin problem using semiconductor quantum dots. We focus on the interaction between 10^4 – 10^6 nuclear spins and a spin of a single electron or valence-band hole. We also review the experimental techniques as well as the key theoretical ideas and the implications for quantum information science.

Owing to the progress in fabrication and new experimental techniques^{1–8}, optical and electrical manipulation of spins of single electrons and valence-band holes in semiconductor quantum dots (QDs) has now become possible, potentially enabling the realization of spin qubits for quantum information processing⁹. The spin of the confined electron in a QD experiences the hyperfine interaction with 10^4 – 10^6 nuclear spins^{10–14}. This interaction is usually quantified using an effective Overhauser magnetic field, B_{nuc} , reaching in some cases a few tesla for a highly polarized nuclear spin system¹², with a statistical fluctuation $\sigma_{B_{\text{nuc}}}$ of a few millitesla^{13,14}. The presence and dynamic properties of the Overhauser field thus have a marked impact on the behaviour of the electron spin, and accordingly have received close attention in the quest for realization of a QD spin qubit. Beyond the active research into a quiescent and controllable magnetic environment in solids, nuclear spins themselves have been suggested as a resource with extended coherence (potentially in the millisecond range) useful for quantum information processing¹⁵. Very high nuclear polarization degrees now routinely achievable in QDs have also enabled nuclear magnetic resonance (NMR) to be realized in single QDs^{12,16–18}, which can be applied for non-invasive probing of chemical composition and strain in the volume occupied by the confined electron¹⁹.

Here we review the most pronounced manifestations of nuclear magnetism with a focus on experiments in individual epitaxial and lithographic III–V semiconductor QDs. We will discuss ways to detect and manipulate nuclear spins in both optical and electrical measurements, with one of the important goals being reducing the randomness in the nuclear field. We also discuss how the effect of the hyperfine interaction differs for the case of valence-band holes compared with electrons. Furthermore, we review NMR experiments in small ensembles of nuclear spins in single QDs. Finally, we will briefly outline imminent future directions in nuclear magnetism research in semiconductor nanostructures.

Hyperfine interaction and detection of nuclear polarization

We start with a brief introduction to electron–nuclear spin interaction, description of typical QD structures and ways to detect nuclear spin polarization by optical means and electrical probing.

Hyperfine interaction. The dominant contribution to the electron–nuclear hyperfine interaction originates from the contact Fermi interaction^{13,14} (the hole–nuclear spin interaction is dipole–dipole in nature as described below). The electron–nuclear hyperfine interaction results in a static effect contributing to the energies of the two spin systems, which is usually described in terms of effective magnetic fields: an Overhauser field, B_{nuc} , acting on the electron, a result of interaction with a large number of nuclear spins^{13,14,20}, and a Knight field experienced by individual nuclear spins as a result of interaction with the spin of the localized electron^{13,14,16,21}. Importantly, the hyperfine interaction also leads to a dynamical effect responsible for the transfer of spin between the two systems^{13,14}.

The nuclear field B_{nuc} fluctuates around its average as a result of the redistribution of nuclear spin polarization due to dipolar coupling or through virtual excitations of the electron spin. In the limit of large N , where N is the effective number of nuclei, this can be described by a Gaussian distribution^{10,11} with standard deviation $\sigma_{B_{\text{nuc}}} = B_{\text{nuc}}^{\text{max}}/\sqrt{N}$, where $B_{\text{nuc}}^{\text{max}}$ is the maximum Overhauser field of a few tesla^{22–25}. For an electron confined in a GaAs quantum dot and interacting with a typical number of 10^6 spin-3/2 nuclei, this results in $\sigma_{B_{\text{nuc}}} \approx 4$ mT. The value of $\sigma_{B_{\text{nuc}}}$ can exceed 20 mT in small self-assembled In(Ga)As dots with high concentration of spin-9/2 In. In an experiment with a large number of identical measurements, electron spins initialized in the same state will exhibit different dynamics as they will evolve in a slightly different effective magnetic field. When averaging over many measurements, this will effectively result in spin dephasing on the scale of a typical precession period of the electron in the field of the order of $\sigma_{B_{\text{nuc}}}$: the dephasing time T_2^* is of the order of 15 ns for $\sigma_{B_{\text{nuc}}} \approx 4$ mT (refs 1,5,10,11,26,27). Much of this dephasing due to the random nuclear field can be unwound using spin-echo techniques, because the nuclear field evolves slowly on the timescale of the electron spin dynamics. The remaining decay of the electron spin coherence, with characteristic timescale T_2 , gives information on the timescale of the nuclear field fluctuations^{1,5,26,28–30}.

Detection of nuclear spin polarization in epitaxial quantum dots. We first discuss semiconductor QDs fabricated directly by

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crystal growth techniques using molecular beam epitaxy (MBE) and metal–organic vapour phase epitaxy (MOVPE)⁴¹. Structures with typical in-plane dimensions of 20 to 80 nm and heights of 2 to 10 nm are formed (Fig. 1b), providing strong electron and hole confinement of tens of millielectronvolts. Of particular interest for spin manipulation in optical experiments are neutral (uncharged) and singly charged QDs, possible to obtain in charge-tunable devices³² or in chemically doped samples³³.

Detection of nuclear spin polarization is rather straightforward in photoluminescence of single QDs^{20–24,33–37}. For example, by changing the sign of circular polarization of laser excitation, one can easily observe changes in the Zeeman splitting of the QD bright excitons (Fig. 1d), reflecting the electron Overhauser shift. In most cases, determination of the absolute degree of nuclear polarization is a difficult task, as it requires accurate knowledge of the QD chemical composition^{19,22}. Thus, it is more practical to operate in terms of Overhauser shifts, which can be measured in photoluminescence with an accuracy of a few microelectronvolts, and can be converted to Overhauser fields, B_{nuc} , if the electron g -factor g_e is known. Similarly to photoluminescence, in resonant optical measurements on single dots, such as differential transmission³⁸ or resonance fluorescence³⁹, the Overhauser shifts can be measured with high accuracy. In measurements on ensembles of QDs, the average degree of nuclear polarization can be extracted either from detailed analysis of photoluminescence polarization⁴⁰ or from ultrafast optical measurements of the Larmor precession of electrons⁴¹.

Detection of nuclear spin polarization in gate-defined dots.

A lithographic QD is formed in a two-dimensional electron gas (2DEG) hosted by a GaAs/AlGaAs heterostructure^{20,42–44} (Fig. 2a). Surface gates on top of the heterostructure are used to deplete the 2DEG locally, which makes it possible to control the electron number in the formed QDs, the tunnel coupling between neighbouring QDs, and the tunnel coupling between the QDs and reservoirs. Typical dimensions of these dots are 40 nm in the plane and 10 nm in the growth direction. Gate-defined dots are probed electrically either by measuring electron transport through the QD (or through several dots in series), or by directly probing the charge state of the QD using a nearby charge detector^{20,42}.

Analogously to the case of optical measurements, the nuclear polarization along the external magnetic field B_{ext} can be probed by measuring the shift induced by B_{nuc} in the total electron Zeeman splitting, E_{ez} . This can be measured, for instance, through electron spin resonance (ESR)^{2,45} or electric-dipole spin resonance (EDSR)^{46,47}. The width of the resonance peak measured with sufficiently long time averaging gives $\sigma_{B_{\text{nuc}}}$ directly in the absence of dynamic nuclear polarization (DNP) and a bound on $\sigma_{B_{\text{nuc}}}$ when DNP is present. An alternative to spectroscopic measurements is to observe directly how the time evolution of the electron spin is affected by the nuclear field. For instance, the Larmor precession frequency of a single spin precessing about a static magnetic field is modified by $g_e\mu_B B_{\text{nuc}}/\hbar$ (where μ_B is the Bohr magneton and \hbar is Planck's constant). If B_{nuc} fluctuates over time, a time-averaged measurement of the electron spin precession will contain a spread of precession rates, leading to decay of the envelope with a time constant $T_2^* = \hbar\sqrt{2}/(g_e\mu_B\sigma_{B_{\text{nuc}}})$ (ref. 26), where \hbar is the reduced Planck constant.

E(D)SR or electron spin precession is commonly detected by observing the lifting of the so-called Pauli spin blockade^{42,48} (Fig. 2c). This blockade occurs at the transition between the (1,1) and (0,2) charge regions in a double quantum dot, where tunnelling is only allowed for spin-singlet states, but blocked for triplets ((n,m) refers to n and m electrons in adjacent dots). If E(D)SR flips the spin of one of the electrons of a triplet, the blockade is lifted. Pauli blockade is also directly used to access the average B_{nuc} , the difference of the nuclear field in the two dots, ΔB_{nuc} , and the uncertainties in these two quantities. For instance, the blockade is lifted at a

crossing of two states with different spin, where electron–nuclear flip-flops mix the spin states without energy cost. Hence, the detuning ε at which the $m = 1$ triplet T_+ crosses the singlet branch S (Fig. 2d)⁴⁹ can be detected, which depends on $E_{\text{ez}} = g_e\mu_B(B_{\text{ext}} + B_{\text{nuc}})$. Therefore B_{nuc} can be extracted at a given B_{ext} . Another example is to start from the singlet ground state at large positive detuning and initiate oscillations between S and T_0 (the $m = 0$ triplet) with frequency $f = |g_e\mu_B\Delta B_{\text{nuc}}|/\hbar$ by a fast gate voltage pulse to large negative detuning. The decay time of the oscillation gives a measure of $\sigma_{\Delta B_{\text{nuc}}}$. Using single-shot readout, such a measurement of ΔB_{nuc} involving thousands of samples takes less than 10 ms (refs 50,51) allowing real-time tracking of ΔB_{nuc} (Fig. 2e). The time resolution is sufficient to resolve the Overhauser field fluctuations, resulting in a detailed picture of the spin dynamics.

Dynamic nuclear polarization

The hyperfine interaction enables not only sensing of the nuclear magnetic field through measurement of the electron spins, but also manipulation of the nuclear spins via the electron spins: the transverse terms of the hyperfine interaction mediate electron–nuclear flip-flops^{13,14} in which the electron changes its spin by ± 1 with a simultaneous change of the spin of one of the nuclei by ∓ 1 . These flip-flop terms generate DNP when the up versus down spin pumping rates are asymmetric. A steady-state nuclear spin polarization is reached when nuclear spin pumping rates are balanced by nuclear spin relaxation rates. Under most conditions, DNP is weak because nuclear spin pump rates are suppressed owing to the mismatch between the nuclear and electron Zeeman splitting. There are, however, a number of ways, both optical and electrical, to overcome the energy mismatch and to induce a preferential pumping direction.

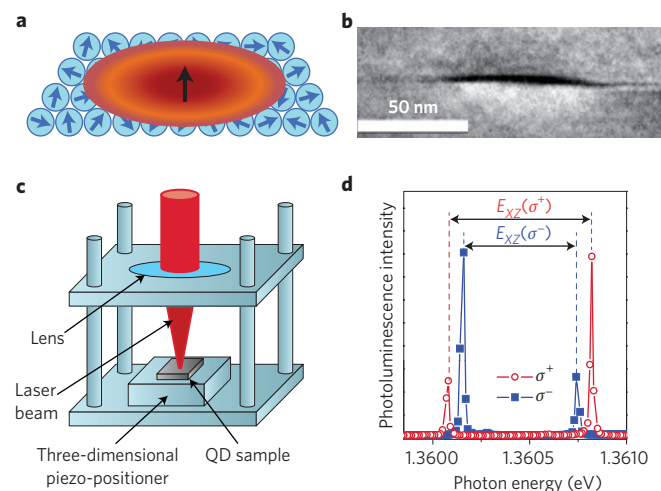


Figure 1 | Optical measurements of nuclear spin effects in quantum dots.

a, A schematic representation of the electron wavefunction in the dot (shown in orange) overlapping with a large number of nuclei (blue circles). Electron spin is shown with a black arrow, and randomly orientated nuclear spins are shown with blue arrows. **b**, Transmission electron microscopy image of an InP/GaInP self-assembled quantum dot, with darker area corresponding to the In-rich region. **c**, A typical micro-photoluminescence set-up. A sample is attached to a three-dimensional piezo-positioner, allowing it to move with respect to a tight laser spot ($\sim 2\ \mu\text{m}$) obtained using a lens with a high numerical aperture. **d**, Micro-photoluminescence spectra measured for a single InGaAs/GaAs QD in an external magnetic field $B_z = 5.3\ \text{T}$ along the QD growth axis, z . Circularly polarized non-resonant optical excitation is used. In both cases dynamic nuclear polarization is apparent, as the exciton Zeeman splitting between the peaks in the spectrum measured with σ^+ polarized excitation (circles), $E_{\text{xz}}(\sigma^+)$, is larger than that for σ^- , $E_{\text{xz}}(\sigma^-)$ (squares).

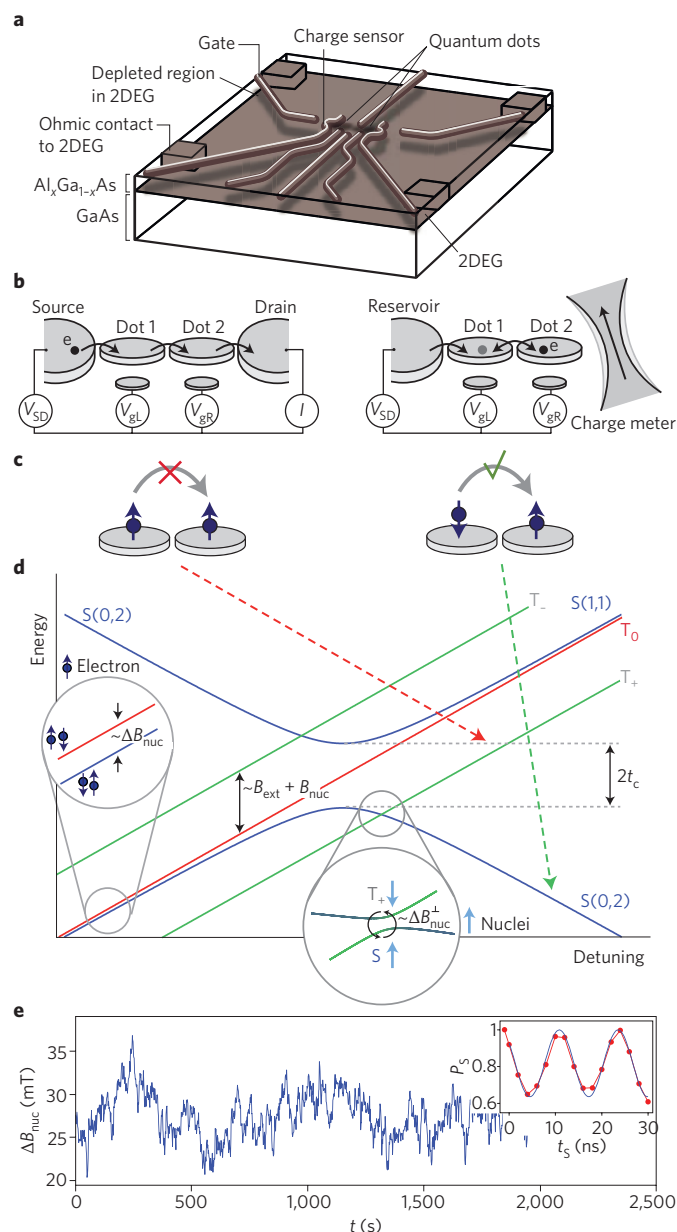


Figure 2 | Electrical probing of nuclear spin effects in gate-defined quantum dots. **a**, Schematic of a gate-defined double QD. **b**, Measurement of the current through a double QD (left) and sensing of the occupation of each dot using a nearby charge detector (right). **c**, Pauli spin blockade is used to convert spin to charge information. The Pauli exclusion principle forbids electrons with parallel spins (spin triplet) to occupy the same dot (left), whereas double occupancy is allowed for spin singlet (right). **d**, Energy levels of a double QD as a function of the relative energy detuning, ϵ , between the (1,1) and (0,2) charge configurations. This detuning can be controlled through gate voltages V_{GL} and V_{GR} in **b**. $S(1,1)$ and $S(0,2)$ denote the spin singlets in (1,1) and (0,2). Because of Pauli exclusion only $S(0,2)$ is relevant in the (0,2) region. Near the transition, $S(1,1)$ and $S(0,2)$ hybridize because of the inter-dot tunnel coupling t_c . $T_+ = |\uparrow\uparrow\rangle$, $T_0 = 1/\sqrt{2}(|\uparrow\downarrow\rangle + |\downarrow\uparrow\rangle)$ and $T_- = |\downarrow\downarrow\rangle$ are the three (1,1) triplets. The states T_+ and T_- split off owing to B_{ext} . Far left in the (1,1) region, the eigenstates turn into $|\uparrow\downarrow\rangle$ and $|\downarrow\uparrow\rangle$ because of the difference of B_{nuc} in the two dots, ΔB_{nuc} (left inset). The degeneracy point of $S = 1/\sqrt{2}(|\uparrow\downarrow\rangle - |\downarrow\uparrow\rangle)$ and T_+ (middle inset) can be used for polarizing nuclear spins. **e**, Time trace of ΔB_{nuc} . Each data point reflects the frequency $g\mu_B\Delta B_{nuc}/h$ of an oscillation between S and T_0 , showing the probability to obtain a singlet P_s (inset). Figure reproduced with permission from: **a**, ref. 43, © 2008 NPG; **e**, ref. 44, © 2010 APS.

There have been many attempts to find an efficient way of achieving DNP^{21–25,33,34,49,52,53}, with the main motivation of achieving 100% polarization of nuclear spins. This would prevent nuclear–nuclear flip-flops and strongly suppress the randomness in the nuclear field and the concomitant electron spin decoherence¹⁰.

Dynamic nuclear polarization in optically pumped quantum dots. Most experiments on optical pumping of nuclear spins in QDs are performed at temperatures below 50 K (normally below 10 K). In most cases DNP occurs following the spin transfer from optically pumped or resident electrons. Electron Overhauser shifts in excess of 100 μeV can be obtained using optical pumping^{22–25,33,34}, and B_{nuc} up to 3 T have been reported^{23–25}. Using rough estimates of the dot composition, degrees of nuclear polarization up to 60% are now routinely obtained.

DNP is readily observed under excitation of QDs with circularly polarized light^{21–25,33–38,54,55}: when σ^+ or σ^- polarized photons are absorbed by the sample, electrons with well-defined spin orientation may be created^{14,56}. This still holds for so-called non-resonant excitation when the laser is tuned up to 100–200 meV above the QD lowest energy levels^{21–25,34,54}. Very efficient nuclear spin pumping also occurs under resonant excitation into the lowest energy states of the dot^{33,38,39,57,58}. This leads to various ‘line-dragging’ effects as the excitation laser is tuned seemingly out of resonance but build up of the Overhauser field maintains the on-resonance condition^{33,38,57–59}.

The efficiency of electron–nuclear spin flip-flops leading to DNP depends on the energy splitting between the initial and final electron (exciton) states involved in the electron spin-flip, $\Delta E_{\uparrow\downarrow}$, and scales roughly as $(1/\Delta E_{\uparrow\downarrow})^2$. The value of $\Delta E_{\uparrow\downarrow}$ may be as large as 0.1–0.5 meV and is a major energy cost of the flip-flop process. Owing to the requirement of the energy conservation, in most cases the spin flip-flop occurs as a second-order process: the electron is virtually transferred to the state with the opposite spin, while a single nuclear spin is flopped; the electron then escapes from the dot (or a trion is formed in a charged dot), the process usually accomplished by emission (absorption) of a photon^{21–25,33–38,54,55} or electron tunnelling from the dot^{55,57,58}. Note that $\Delta E_{\uparrow\downarrow}$ is dependent on both B_{ext} and B_{nuc} . This gives rise to an intrinsic feedback mechanism in the DNP process, which is a source of pronounced bistabilities and switching of nuclear polarization in a QD under optical pumping^{23,24,35,60} (Fig. 3a).

The dynamics of optically induced spin pumping have been studied in pump–probe experiments^{36,38,61–63}. For small B_{ext} (that is, small $\Delta E_{\uparrow\downarrow}$), nuclear polarization build-up time under optical pumping is in the millisecond range^{36,61}, whereas in higher fields of a few tesla, the typical build-up time is of the order of 1–10 s (refs 38,61,63). Nuclear spin depolarization can occur via flip-flops between interacting (neighbouring) nuclei, giving rise to nuclear spin diffusion. In most QDs, however, the nuclear Zeeman splitting matching required for such nuclear–nuclear flip-flops is not fulfilled, owing to quadrupole interactions occurring mainly as a result of strain^{13,19,60,64–66}. Thus nuclear spin diffusion is typically suppressed in QDs^{36,60,61,63}. The presence of strain and hence strong quadrupole effects is one of the main reasons that DNP is possible in zero external magnetic field^{21,33,36,61,67}, where nuclear polarization lifetimes in the dark of up to tens of seconds have been observed^{36,61}. Remarkably, in magnetic fields of a few tesla, nuclear polarization in strained self-assembled dots survives as long as 30 h (refs 36,60,61). In contrast, if a QD is brought in contact with an unpolarized electron reservoir, as is often the case in charge-tunable devices, nuclear spins are depolarized in a few milliseconds³⁶.

Dynamic nuclear polarization in gate-defined quantum dots. The first observation of DNP in gated quantum dots was reported in 2004 by Ono *et al.*⁶⁸, manifesting itself in hysteretic magnetic field sweeps (Fig. 4a) and slow oscillations of the leakage current through

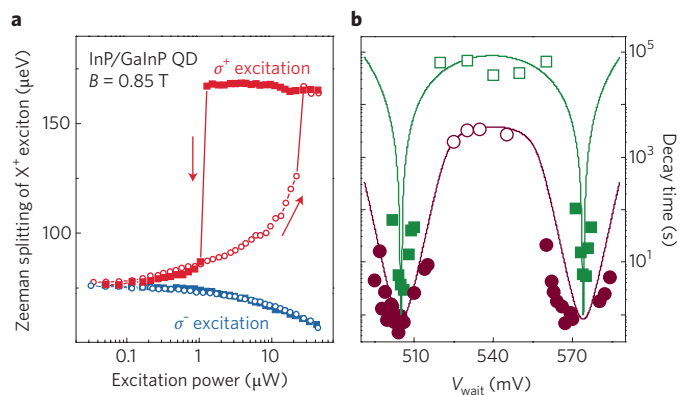


Figure 3 | Dynamic nuclear polarization in optically pumped quantum dots. **a**, Bistable behaviour of nuclear polarization in a positively charged InP/GaInP quantum dot pumped non-resonantly with circularly polarized light in external magnetic field along the growth axis $B_z = 0.85$ T. The plot shows the Zeeman splitting of the positively charged exciton, X^+ , measured in photoluminescence as the laser excitation power is scanned from high to low and back. Directions of the scans are shown with arrows for σ^+ pumping, inducing Overhauser field B_{nuc} (felt by optically excited electrons) antiparallel to B_z and leading to the reduction of the electron Zeeman splitting. This causes positive feedback for DNP and results in switching and bistability of B_{nuc} (refs 23,24,35). In contrast, under σ^- pumping, B_{nuc} is parallel to B_z , causing the slow-down of DNP as B_{nuc} increases. **b**, Decay times for nuclear spin polarization in an InGaAs QD in a Schottky diode as a function of bias measured at temperatures of 4 K (dark red) and 0.2 K (green) and $B_{\text{ext}} = 5$ T. The decay of the Overhauser field is mediated by the electron cotunnelling between the dot and the electron reservoir in the contact, particularly pronounced at the edges of the charging plateau around 505 and 575 mV in this graph. The decay time increases up to 10⁵ s for $T = 0.2$ K at biases away from the cotunnelling regime. Panel **b** reproduced with permission from ref. 60, © 2011 APS.

a double quantum dot in the spin blockade regime. In the same regime, several experiments report hysteresis^{52,69} and bistable current behaviour⁶⁹. Polarization up to about 40% has been claimed⁵². The complexity of the interplay between nuclear spin polarization and transport in the spin blockade regime has triggered a large amount of theoretical work^{70–74}. Although in the experiments many details of the observed behaviour are not understood, all have in common that a degeneracy of two-spin states with different spin, such as S and T_+ (the $m = 1$ triplet) and S and T_- (the $m = -1$ triplet) seems to be the main origin of electron–nuclear flip-flops (Fig. 4c). At these crossings, electron–nuclear flip-flops are possible at no energy cost.

Compared with these transport measurements, experiments with specially designed gate voltage pulse cycles offer a more controlled way to realize a DNP pump scheme. In ref. 49, the system is first initialized in the $S(0,2)$ state and subsequently an adiabatic sweep across the $S-T_+$ degeneracy point (Fig. 2d and 4c) transfers up to one unit of angular momentum into the nuclear spin bath. Finally, one electron is pushed out of the double dot and the next cycle begins. Spin transfer in the opposite direction and thus full bidirectional control (Fig. 4c) was demonstrated⁵³ by initialization of a $T_+(1,1)$ state followed by a similar slow passage through the $S-T_+$ degeneracy point. These pump cycles can be extended to reduce fluctuations of the hyperfine field^{44,45}.

Rather than exploiting level degeneracies, the energy for electron–nuclear flip-flops can be provided by a resonant a.c. electric field (inset to Fig. 4b). The electric field modulates the hyperfine coupling constant of each nucleus to the electron and therefore the transverse term of the hyperfine coupling. This directly drives electron–nuclear flip-flops^{45,47} (Fig. 4b).

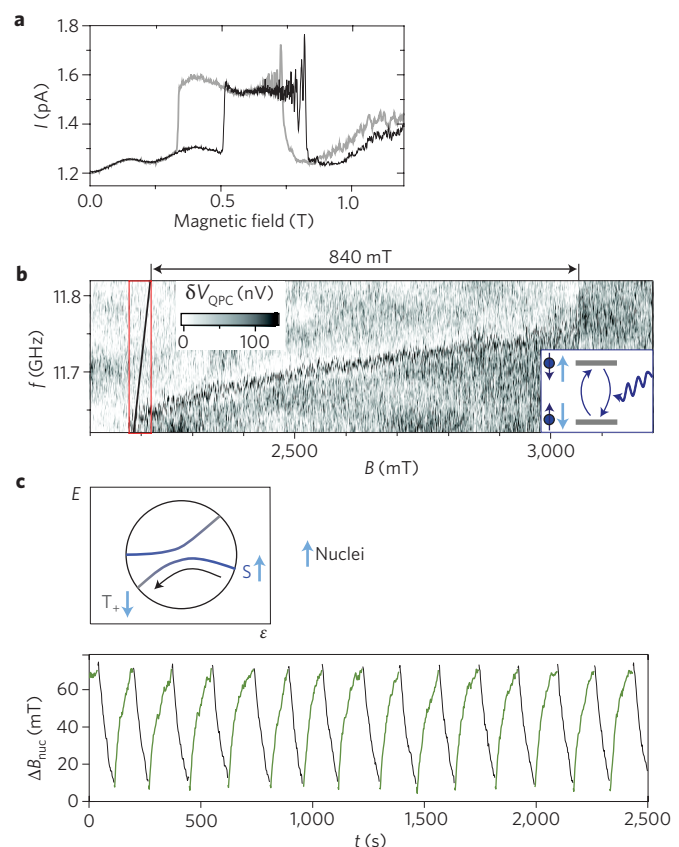


Figure 4 | Dynamic nuclear polarization in gate-defined quantum dots.

a, DNP leads to a hysteric leakage current in the spin blockade regime as a function of increasing and decreasing magnetic field. **b**, Average charge occupation of a double quantum dot in the spin blockade regime (measured via the change in voltage across the quantum point contact (QPC) sensor, δV_{QPC}) under the influence of an alternating electric field. When the excitation frequency f is resonant with the electron Zeeman splitting, it drives electron–nuclear flip-flops (inset), thus lifting the spin blockade and changing the average occupation (darker regions). As the field B_{ext} (directed along z) is swept upwards, a nuclear polarization partly counteracts the change of B_{ext} , thus moving the resonance away from its equilibrium position (black diagonal line) by up to 840 mT. **c**, Control of the hyperfine field gradient in a double quantum dot operated as an $S-T_0$ qubit. DNP is obtained by sweeping the detuning through the $S-T_+$ transition (top), causing spin transfer between electrons and nuclei. Each data point on the lower panel reflects a measurement of ΔB_{nuc} as shown in the inset to Fig. 2e. DNP pulses were applied between successive measurements. They increase or decrease ΔB_{nuc} depending on whether the DNP cycle starts from an S (green) or T_+ state (black). Figure reproduced with permission from: **a**, ref. 68, © 2004 APS; **b**, ref. 47, © 2007 APS; **c**, ref. 44, © 2010 APS.

We now discuss nuclear spin dynamics in gate-defined QDs, which can be measured accurately using fast manipulation of the electron spin by gate voltages. Here, two different pictures of the nuclear spin dynamics are useful. At short times, the fluctuations of the Overhauser field are determined by the hyperfine interaction and the nuclear Larmor precession, whereas at longer times ($>10^{-4}$ s), nuclear flip-flops due to the dipolar coupling lead to a diffusion-like redistribution of the local nuclear polarization inside and outside the quantum dot¹¹.

The diffusive long-time behaviour has been probed by directly measuring the fluctuations of the Overhauser field^{75,76} using methods discussed above (Fig. 5a). At low magnetic fields (below about 20 mT), one finds roughly a 10-fold speeding up of spin diffusion⁷⁵ that probably reflects the activation of additional diffusion channels

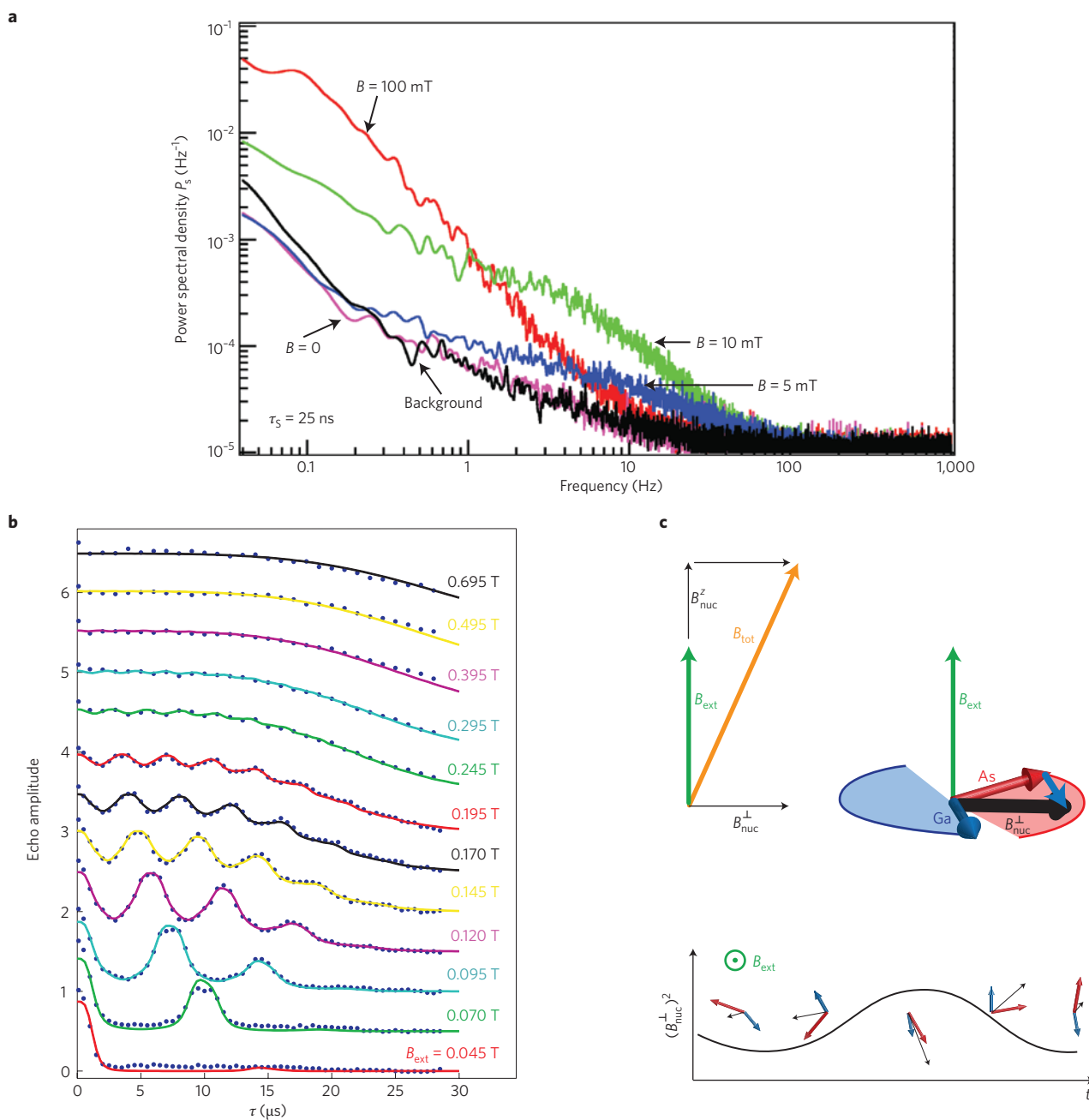


Figure 5 | Dynamics of nuclear spins in a gated double-dot structure. **a**, Spectra of the fluctuation of the nuclear hyperfine field at relatively low frequency, obtained from time traces of the singlet probability P_s of the qubit after precession in the Overhauser field over a fixed evolution time τ_s . A significant speeding up of the dynamics is observed at low magnetic fields. The shape of the spectrum can be explained in terms of nuclear spin diffusion. **b**, Hahn-echo signal in a S-T₀ qubit as a function of the total evolution time, τ , for different values of magnetic field. Exchanging the two electrons at time $\tau/2$ via a gate voltage pulse causes them to see the same static hyperfine field, so that only fluctuations during τ reduce the probability of the electrons to return to their initial state, which is reflected in the echo amplitude. Curves are offset for clarity and normalized. Data are shown as dots, fits as solid lines. **c**, Illustration of the semiclassical model used for the fits (see main text). Figure reproduced with permission from: **a**, ref. 75, © 2008 APS; **b,c**, ref. 28, © 2010 NPG.

by the reduced Zeeman energy mismatch, such as electron-mediated spin transfer between nuclei. The electron-mediated diffusion also leads to a dependence of the decay rate of an induced polarization on the occupancy of the dot⁷⁶. Gate-defined QDs are usually made of unstrained GaAs; therefore quadrupole effects are weak and were neglected in the discussion above.

The short-time nuclear spin dynamics have been probed via electron-spin dephasing under inversion of the electronic state halfway through an interval of free evolution⁷⁷, a procedure known as Hahn echo. This technique is only sensitive to the relatively fast

changes of the Overhauser field during the evolution. Measuring the final electronic state gives detailed insight into the nuclear spin dynamics on the microsecond timescale²⁸ (Fig. 5b,c). The monotonic decay of the Hahn-echo signal with characteristic evolution time, τ , at high fields is a result of the diffusive dynamics of B_{nuc}^z due to dipolar coupling. The resulting spectral diffusion is predicted to cause a $\exp[-(\tau/T_{\text{SD}})^4]$ decay of the echo^{78,79} with a characteristic time constant T_{SD} of a few tens of microseconds.

The oscillations found at lower fields, which eventually turn into full collapses and revivals, were first predicted based on a fully

quantum mechanical treatment⁷³ but can also be understood with a semiclassical model. It is based on the electronic Zeeman energy splitting being proportional to the total magnetic field

$$B_{\text{tot}} = \sqrt{(B_{\text{ext}} + B_{\text{nuc}}^z)^2 + (B_{\text{nuc}}^\perp)^2} \approx B_{\text{ext}} + B_{\text{nuc}}^z + (B_{\text{nuc}}^\perp)^2 / (2B_{\text{ext}})$$

(Fig. 5c, top left). Dephasing is caused by fluctuations of this level splitting and thus related to the time-dependence of both the parallel and transverse nuclear components, B_{nuc}^z and $(B_{\text{nuc}}^\perp)^2$. The collapses and revivals observed in the electron spin echo signal arise from the phase associated with $(B_{\text{nuc}}^\perp)^2$. The transverse nuclear field, $\mathbf{B}_{\text{nuc}}^\perp$, is a vector sum of contributions from the three nuclear species ⁶⁹Ga, ⁷¹Ga and ⁷⁵As (Fig. 5c, top right). Owing to the different precession rates of these species, $(B_{\text{nuc}}^\perp)^2$ thus oscillates at the three relative Larmor frequencies (Fig. 5c, bottom). The amplitude and phase of the oscillating nuclear fields fluctuate over the course of many repetitions, thus leading to randomization of the resulting phase and suppression of the echo signal. If, however, the precession interval is approximately a multiple of all three Larmor periods, the oscillations imprint no net phase on the electron spin and the echo amplitude revives. A quantitative model treating the components of $\mathbf{B}_{\text{nuc}}^\perp$ as classical variables also explains the faster decay of the echo envelope at low fields (Fig. 5b) in terms of dephasing of the nuclear spins themselves.

Interaction of valence-band holes with nuclear spins

Unlike electrons having *s*-type atomic wavefunctions, the hole has a wavefunction constructed predominantly from *p* orbitals with zero density at the nuclear site. This leads to a vanishing contact part of the hyperfine interaction, which combined with extended hole spin lifetimes in QDs⁸⁰ presents holes as a potentially viable alternative to electrons for implementation of spin qubits^{80,81}. Recent theory predicts that the hole hyperfine interaction, dipole–dipole in nature, can be as large as 10% of that of the electron, and is strongly anisotropic^{82–85}. Furthermore, heavy-hole (hh) states with pure *p* symmetry couple only to the nuclear field along *z*; that is, they exhibit an Ising-type interaction with nuclear spins and slow decoherence^{83,84}. On the other hand, it has been shown theoretically that

the hyperfine interaction leads to efficient decoherence of the pure hh states having an admixture of *d* orbitals in the wavefunction, estimated to be considerable (for example, around 20% for Ga) from recent experiments⁸⁶. Another decoherence mechanism arises from heavy–light hole mixing, as light-hole (lh) states couple to all nuclear spin components^{83,85}. In most QDs studied, however, hh–lh mixing is very small^{80,81}, so this decoherence mechanism should in principle manifest itself in rare cases^{83,85,87}, whereas the contribution of *d* orbitals is common for III–V semiconductors and will play an important role in a broad class of III–V nanostructures⁸⁶.

Experimental evidence for the hole hyperfine interaction can be obtained from the measurements of the hole spin dynamics. Ensembles of p-doped self-assembled InGaAs/GaAs QDs were studied in low longitudinal magnetic fields B_z using ultrafast optical pump–probe measurements^{85,87} and spin noise spectroscopy⁸⁸. Suppression of the hole spin dephasing in refs 85 and 87 and sharp increase of the hole spin correlation times in ref. 88 were found above a characteristic $B_z = 2.5$ –3 mT. This gives an estimate of the magnitude of the fluctuating transverse nuclear field acting on the hole spin, about an order of magnitude lower than that for electrons in similar QD samples⁸⁷. The presence of the longitudinal nuclear field can also be evidenced using spin noise detection⁸⁸ (Fig. 6a).

Measurements on individual QDs using optical detection with high spectral resolution enabled the hole Overhauser shift to be measured directly and simultaneously with that for the electron^{33,39}. The ratio between the all-element-averaged hole (*C*) and electron (*A*) hyperfine constants was found to be $C/A \approx -0.1$ in InP and InGaAs QDs^{33,39,86}. Further studies combining optical and radiofrequency techniques revealed that the $|C/A|$ ratio can reach 0.15–0.2, and that $C > 0$ for anions (As, P) and $C < 0$ for cations (In, Ga)⁸⁶. The sign difference was explained by the contribution of atomic *d* orbitals to the cationic hole Bloch wavefunction, whereas for anions the wavefunctions is purely *p*-type.

Understanding of the hole spin decoherence and the role of the hole hyperfine interaction may still be incomplete. There is a rather large spread of measured dephasing times T_2^* for the hole spin: over 100 ns using coherent population trapping³ and 2 to 20 ns in ultrafast optical measurements of the hole spin Ramsey fringes^{6–8}.

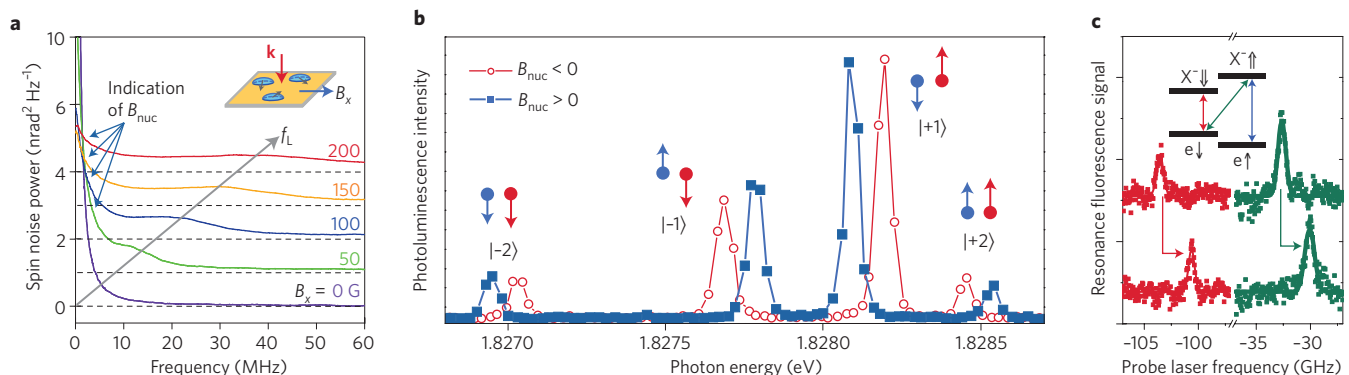


Figure 6 | Hole-nuclear spin interaction in optically pumped quantum dots. **a**, Hole spin noise in transverse applied magnetic fields (B_x). A finite noise component remains at zero frequency. This reveals the presence of the longitudinal (along *z*) components of the nuclear Overhauser magnetic field acting on holes. Peak in the hole spin noise is also observed around the hole Larmor frequency f_L . **b**, Photoluminescence spectra of a single neutral InP/GaNP QD at $B_z = 6$ T for negative (blue) and positive (red) nuclear spin polarization induced optically on the dot. Bright ($|\pm 1\rangle$) and dark ($|\pm 2\rangle$) excitons are observed and the corresponding spin orientations of the electron (blue) and hole (red) are shown schematically. The change in the splitting between the bright $|\pm 1\rangle$ and dark $|\pm 2\rangle$ states corresponds to the hole (electron) Overhauser shift. By comparing these shifts, the ratio between the electron and hole hyperfine constants can be extracted. **c**, Inset: laser excitation scheme for measurements of the hole hyperfine constant in a negatively charged dot in magnetic field. Three lasers are shown: (i) polarizing nuclei via an allowed transition and driving the resonance fluorescence (blue); (ii) probing the other allowed transition (red); (iii) probing weakly allowed transition (green). When 'red' or 'green' lasers are on resonance with the $e-X^-$ transitions, resonant enhancement of fluorescence is detected, shown with red and green symbols, respectively. The hole (electron) hyperfine shift can be extracted from the difference between (sum of) the shifts of the 'red' and 'green' peaks as the nuclear polarization on the dot is varied by adjusting the frequency of the blue laser. The two sets of data at the top and bottom of the plot are measured for two different degrees of nuclear polarization on the dot. Figure reproduced with permission from: **a**, ref. 88, © 2012 APS; **b**, ref. 37, © 2011 APS; **c**, ref. 39, © 2010 APS.

It is also an emerging paradigm that electrical noise in the diodes comprising hole-charged QDs may be a factor strongly limiting the T_2^* values^{6,7}.

Narrowing of nuclear field distribution in 'closed-loop' DNP

The preceding sections discussed experiments where angular momentum is transferred from the local electron spin to the nuclear spin bath in an open-loop mode. As a result, the nuclear field was always subject to statistical fluctuations. Here we present a development of the past few years, realized by both optical and electrical means: closed-loop control of the nuclear field, suppressing its randomness to well below the statistical fluctuations. The suppression of the bath fluctuations immediately leads to extended dephasing times and better control of the time evolution of the central spin.

Suppression of nuclear spin fluctuations using optical pumping with feedback. In optically pumped self-assembled dots, such suppression of nuclear spin fluctuations using 'active' stabilization has been achieved by resonant continuous-wave^{27,38} and pulsed⁴¹ laser excitation. The stabilization was achieved via feedback reversing any changes in the nuclear polarization so that the QD optical transition remained in resonance with the continuous-wave laser^{27,38}, or spin precession of the QD electron remained synchronized with the pulse repetition rate of the ultrafast laser⁴¹. In all of these experiments, low or moderate degree of nuclear spin polarization was achieved, in contrast to the previous requirement (as it was then considered) of nearly 100% nuclear polarization to suppress nuclear spin fluctuations¹⁰.

Greilich *et al.*⁴¹ used Faraday rotation in ensembles of electron-charged self-assembled InGaAs dots. Electron spin precession in a large number of dots becomes synchronized with the repetition rate of the laser by means of DNP and despite the initial ensemble spread of the electron g factors. Deviation from the synchronization condition, caused, for example, by nuclear spin fluctuations, would lead to increased light absorption in the dot, which in turn would lead to nuclear spin pumping until the nuclear spin projection along the in-plane external field was restored to fulfil the synchronization condition⁸⁹.

Latta *et al.*³⁸ presented measurements showing the damping of fluctuations in the optical transition energy in a single QD by locking the quantum-dot resonance to the incident laser. The locking was achieved by DNP, which also resulted in the 'line-dragging' and a marked distortion of the QD line-shape in differential transmission³⁸. As the model simulations show, the optical transition stabilization occurring as a result of DNP is accompanied with a significant narrowing of the Overhauser field variance.

Xu *et al.*²⁷ observed enhancement of the electron T_2^* using coherent dark-state spectroscopy carried out on a single electron-charged dot. This effect was explained by suppression of nuclear spin fluctuations under the Overhauser field locking similar to the line-dragging in ref. 38. A marked enhancement of the electron T_2^* by a factor of several hundred, arising as a result of suppressed nuclear spin fluctuations, was observed.

Narrowing in gate-defined dots. In gate-defined dots, several distinct approaches to suppress nuclear field fluctuations have been successfully used. The conceptually simplest possibility for suppressing the randomness of the Overhauser field (or its gradient) is to rapidly measure it and to use DNP to restore its desired value. For S- T_0 qubits, this approach⁴⁴ permitted a reduction of the root-mean-square fluctuations of the hyperfine field gradient, $\sigma_{\Delta B_{\text{nuc}}}$, by about a factor of 2. A more powerful approach relies on directly conditioning the spin transfer from the electrons to the nuclei on the current value of the hyperfine field, thus letting the electron spin itself act as a complete feedback loop not requiring external intervention. This approach was used to control both the hyperfine field in the

individual halves of a double quantum dot using an ESR-based spin transfer technique⁴⁵, and the field gradient ΔB_{nuc} between the two dots of an S- T_0 qubit through exchange-mediated spin transfer⁴⁴.

Such feedback schemes can be understood from the 'pumping curve', which provides the polarization rate as a function of the current value of the hyperfine field. Figure 7 shows pumping curves for both feedback methods. A stable fixed point is obtained whenever the pumping curve crosses zero with a negative slope so that fluctuations away from the fixed point are corrected by an opposing pump effect.

The ESR pumping curve (Fig. 7a) emerges from the resonance condition of the microwave excitation with the Zeeman field $B_{\text{ext}} + B_{\text{nuc}}$ seen by the electron, with the overall negative background slope arising from relaxation of the nuclear spin polarization⁴⁵. The narrowing effect was inferred from dragging and locking of the ESR resonance frequency in response to changes of the externally applied field (Fig. 7b), which were found to be compensated by nuclear polarization such that the total field remained constant⁴⁵.

The oscillatory behaviour of the corresponding pumping curve for the S- T_0 qubit (Fig. 7c) was generated by initializing it in S and then letting it precess between S and T_0 for a time τ_{FB} under the influence of ΔB_{nuc} (ref. 44). Upon subsequently sweeping the gate voltages across the S- T_+ transition, a nuclear spin can only be flipped by the S-component of the qubit state emerging from the evolution. Thus, the average pump rate is proportional to the ΔB_{nuc} -dependent singlet probability. The stabilizing effect of this feedback scheme was demonstrated by measuring the S- T_0 qubit precession: narrowing of the ΔB_{nuc} distribution (Fig. 7d,e) and a corresponding enhancement of the qubit's T_2^* from 16 ns to at least 150 ns were observed.

It was reported earlier⁹⁰ that the same type of DNP without feedback could extend T_2^* to beyond 1 μs . Although theoretical scenarios⁹¹ have been proposed to explain such an effect⁹⁰, it later turned out that another interpretation of the data was much more plausible⁹².

Nuclear magnetic resonance in single quantum dots

Direct manipulation of nuclear spins using NMR is desirable for several reasons. As in the previous sections, this provides new insights in the spin properties of QD electrons and holes. NMR measurements provide information on the nuclear spin coherence, an important insight in the properties of the magnetic environment of the electron and hole spin-qubits. Pulsed NMR may also serve as a tool for fast redirection of the large Overhauser fields inside the dot, an additional tool for qubit control¹⁷. Finally, NMR can be used to reveal the structural properties of the dot to provide direct correlations with its electronic properties and feedback for QD fabrication.

The Hamiltonian for a nuclear spin I having a gyromagnetic ratio γ can be written as^{13,66}:

$$H_{\text{nuc}} = -\hbar\gamma I_z + H_Q$$

where $\nu_L = \gamma B_z/(2\pi)$ is the nuclear Larmor frequency, I_z the z -projection of the nuclear spin, and H_Q describes the interaction of the nuclear quadrupole moment with the electric field gradient. The interaction H_Q arises in quantum dots as a result of strain or alloy fluctuations, and is particularly pronounced in self-assembled QDs. In a magnetic resonance experiment transitions between spin states with $\Delta I_z = \pm 1$ are induced with a transverse magnetic field oscillating at a radiofrequency close to ν_L . The corresponding changes in the nuclear spin state populations are detected using optical or electrical methods from changes in the electron Overhauser shift in QDs.

First NMR in QDs was carried out in optical measurements on single GaAs/AlGaAs interface dots¹², where quadrupole effects were weak. The discrete exciton energy structure in QDs was successfully used: changes in the electron Overhauser shift induced by

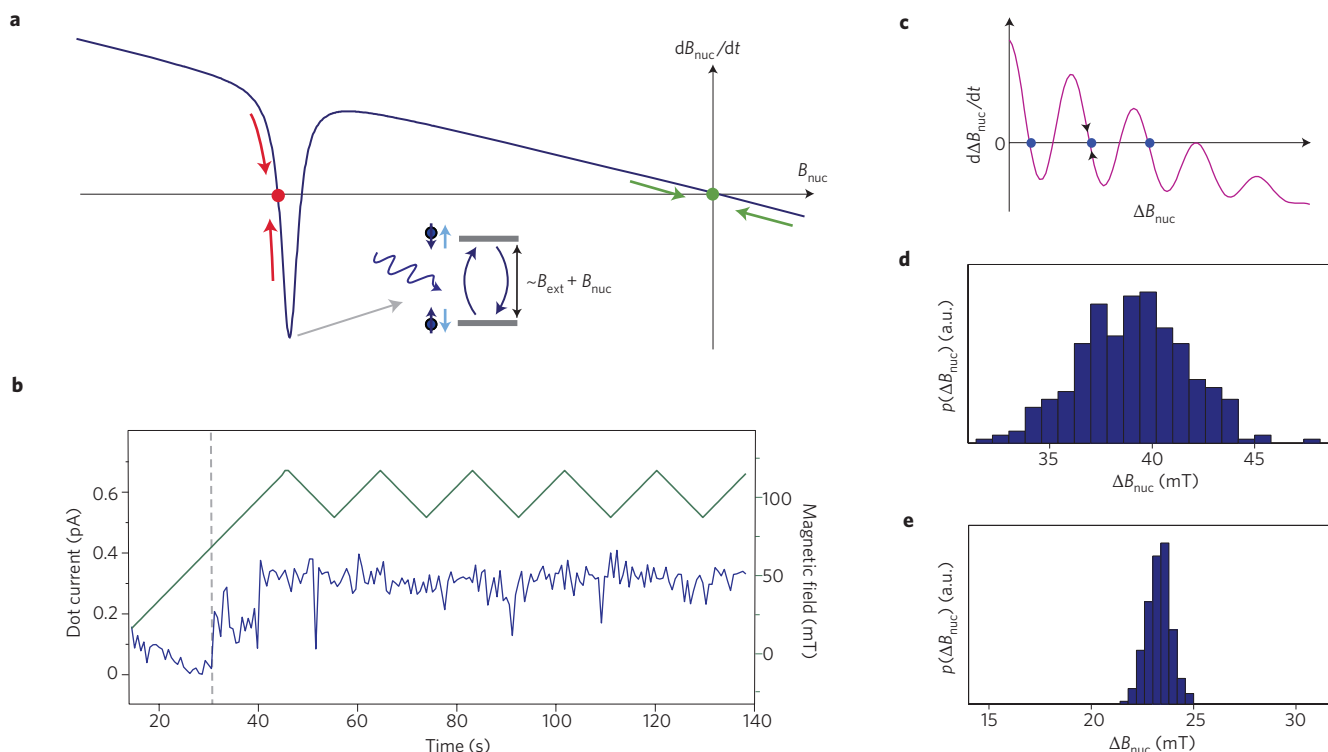


Figure 7 | Nuclear spin narrowing experiments in gate-defined quantum dots. **a**, Schematic illustration of the pumping curve for ESR-based feedback on a single electron spin⁴⁵. Fluctuations away from the fixed points are compensated by a restoring pump effect (arrows). **b**, Polarization dragging experiment for single electron spins using ESR. As the magnetic field (green, right axis) increases from near zero, the singlet-triplet mixing is suppressed while the continuous-wave ESR signal is off-resonant and has no effect. At $B_{\text{ext}} \approx 70$ mT, a resonance condition is met, thus breaking spin blockade (current is shown in blue, left axis). Subsequently, the resulting high current condition is maintained even while sweeping B_{ext} up and down, thus demonstrating the locking of the total field $B_{\text{ext}} + B_{\text{nuc}}$ to the resonance frequency: any change in B_{ext} is compensated by an opposite change in the nuclear polarization. **c**, Pumping curve for voltage pulse based feedback on an S- T_0 qubit. The oscillatory structure arises from first letting the qubit precess in the hyperfine field and then executing a DNP step that is conditional on the state emerging from this evolution. **d**, Distributions of the gradient nuclear field ΔB_{nuc} for fixed pumping, obtained by histogramming instantaneous values of ΔB_{nuc} . The pumping produces a finite mean, but does not substantially change the width of the distribution. **e**, Same measurement, but with feedback pumping applied between measurements, which narrows the distribution. Because the width includes a measurement uncertainty of the instantaneous value of ΔB_{nuc} , the improvement of the dephasing time T_2^* is larger than inferred from the distribution. Figure reproduced with permission from: **b**, ref. 45, © 2009 NPG; **c–e**, ref. 44, © 2010 APS.

radiofrequency excitation could be measured with accuracy of a few microelectronvolts. NMR spectra were measured by simply stepping radiofrequency through the resonance^{12,16}. Further advancement of the nuclear spin control was made possible by using pulsed NMR measured optically¹⁷ in a single GaAs/AlGaAs QD (Fig. 8a,b) and electrically¹⁸ in double GaAs/AlGaAs QD devices. Using such techniques the fast coherent rotations of nuclear spins under the influence of the radiofrequency and external field could be resolved, and the nuclear spin coherence time was measured¹⁷. Rabi oscillations, Ramsey fringes, spin-echo measurements and, finally, arbitrary rotations of large Overhauser fields about any axis on a timescale of a few tens of microseconds were demonstrated¹⁷.

Techniques developed for strain-free GaAs dots have been found inapplicable in self-assembled QDs with strong quadrupole broadenings⁶⁶ due to low NMR signal. Enhancement of NMR signal was achieved in large ensembles of QDs in transverse magnetic fields^{93,94}. Unambiguous interpretation of the experimental data was, however, hampered by the complex spin dynamics⁹⁵, further complicated by the presence of the strong quadrupole effects^{93,94}.

Recently, high-resolution optically detected NMR has been carried out in single self-assembled InGaAs/GaAs and InP/GaInP QDs by using new spin population transfer techniques¹⁹ (Fig. 8c,d). Instead of using a wide radiofrequency band to increase the number of affected nuclear spin transitions, an ‘inverted’ radiofrequency spectrum was used that had two very broad bands (~ 10 MHz) with

a gap in between. This approach led to signal enhancement, for 9/2 spins, of more than a factor of 100 compared with the standard saturation techniques, and allowed measurements with resolution down to about 10 kHz (ref. 19). These techniques reveal a wealth of structural information such as chemical composition and strain distribution in the volume of the wavefunction of the confined electron¹⁹, and present a powerful microscopy tool for non-invasive structural analysis of single QDs. To gain an additional enhancement in spatial resolution of NMR, the use of an effective magnetic (Knight) field of the photoexcited electron may be possible¹⁶. The spatial distribution of the Knight field follows that of the strongly localized electron wavefunction: Knight field gradients of the order of 10^3 T cm⁻¹ can be achieved, potentially enabling determination of the nuclear spins position with resolution of 1 nm inside a single QD¹⁶.

Future directions and other materials

The above sections present the state-of-the-art in nuclear magnetism in semiconductor QDs. Below we comment on possible future developments for the field. We also briefly outline other classes of materials where electron–nuclear spin interactions have been investigated.

Control of nuclear spins for realization of coherent spin qubits.

Efforts to achieve quiescent nuclear spins for improving coherence of the central spin (spin qubit) may continue in several directions. From analysis of QD composition using NMR¹⁹, it is now clear that

polarization degrees of 90% or above may be accessible in optically pumped dots^{19,33}. The effect of this on the coherence of electron or hole spin qubit needs to be verified. Alternatively, approaches achieving stabilized nuclear spin distributions are very attractive as they do not require very high polarization degrees.

Another way to achieve suppression of the nuclear spin fluctuations is to realize an ordered nuclear spin state⁹⁶. This in principle can be achieved by cooling nuclear spins to ultralow submicrokelvin temperatures using adiabatic demagnetization, although first attempts in self-assembled dots experienced difficulties owing to strong quadrupole effects⁶⁵. In future, similar experiments could be attempted in unstrained GaAs dots.

Understanding of nuclear spin coherence in strained structures is another direction aimed at achieving quiescent magnetic environment. Recent initial studies showed more robust nuclear spin coherence in structures with strain⁹⁷, also naturally present in self-assembled dots and some nanowires.

Holes remain rather attractive as a spin qubit because their hyperfine interaction is significantly weaker than that of

electrons. Recent studies have opened the way for engineering of the hole–nuclear spin interaction by appropriate choice of QD composition⁹⁶. In this way, improved hole spin qubit control may be obtained, a subject of further studies.

Beyond the semiclassical approximation. In the coming years, we anticipate a new direction in research on quantum dots that takes nuclear spin control into the quantum regime. This is the regime where the nuclear spin state can no longer be captured in terms of a classical nuclear field or probability distribution of nuclear fields, which have been used to describe current experiments. Creating quantum states of the nuclear spin bath can be done using the coupling Hamiltonian between electron and nuclear spins, which implies that the electron will influence the dynamics of the nuclear bath via some quantum back-action. It is thus interesting to explore whether there is an experimentally detectable deviation from classical models that can be unambiguously attributed to the back-action effect.

As a first example that this may be possible, the creation of squeezed states of the nuclear spin bath in quantum dots was recently proposed, using microwave irradiation^{98,99}. In spin squeezing, the uncertainty of one component of the (total) spin is reduced below the uncertainty limit at the expense of increased uncertainty in an orthogonal component¹⁰⁰. Interestingly, it was shown theoretically that sufficiently strong spin squeezing implies entanglement in the spin bath¹⁰¹.

Although harder to achieve with current techniques, proposals also exist for coherent exchange of a qubit state between the quantum dot electron spin and a collective degree of freedom of the nuclear spin bath¹⁵. If realized, this would mean that the nuclear spin system can be used as a long-lived quantum memory, as even simple Hahn-echo decay times of nuclear spins in quantum dots are about 1 ms (refs 17,18). Such a coherent information transfer would require special ‘dark’ nuclear states with a reduced transverse hyperfine field, which in principle can be created through fast DNP. These states are, however, highly sensitive to dephasing of the nuclear spins, and are subject to a fragile balance between hyperfine-mediated spin transfer and dephasing due to the Knight shift¹⁰². A first step would thus be to establish whether such states, which would manifest themselves in a saturation of the nuclear polarization rate, can indeed be created.

Another example is the creation of superradiance effects giving strongly enhanced electron–nuclear flip-flop rates, which could be observed in transport measurements¹⁰³ as well as optical spectroscopy¹⁰⁴. Common to all these examples is the collective effect of a large number of nuclear spins coherently interacting with a single (central) electron spin.

Finally, it remains to be seen how much narrowing procedures can be improved, and whether they will eventually permit access to probe some form of intrinsic free induction decay that arises from the bath dynamics rather than ensemble averaging, as studied theoretically in refs 74 and 79.

Other material systems. Although this Review focuses on III–V semiconducting quantum dots, there has been a handful of other material systems in which the interplay between a central electron spin and the surrounding nuclear and even electron spin baths have been investigated. Prominent examples include carbon nanotubes¹⁰⁵, both natural (with 1% of ¹³C) and 100% ¹³C, phosphorus spins in silicon^{106,107} and Si quantum dots¹⁰⁸, and nitrogen–vacancy centres in diamond¹⁰⁹. Nuclear spin effects are also studied in quantum dots defined in III–V semiconducting nanowires^{110,111}. Although much of the physics discussed in this Review is applicable to these systems, there are a few notable differences. For example, the spin-echo response of phosphorus spins in Si is due to the ²⁹Si host atoms, and is theoretically and experimentally shown to

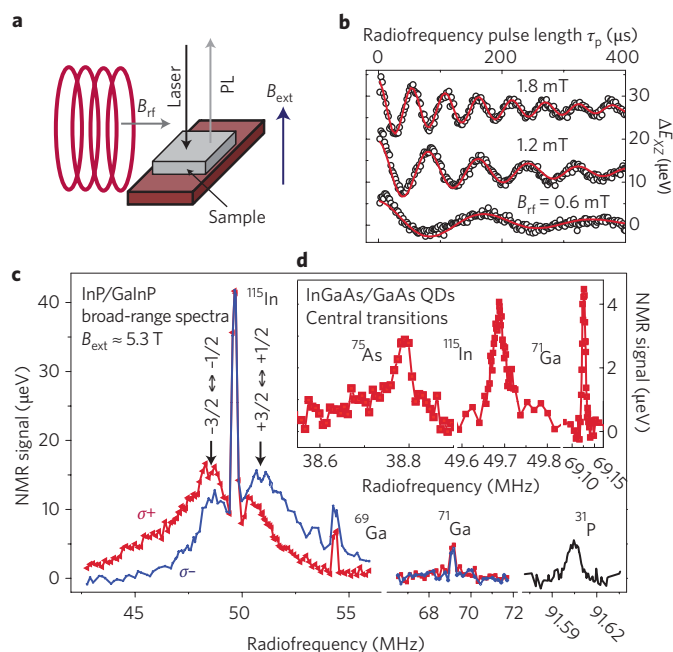


Figure 8 | Optically detected nuclear magnetic resonance in single quantum dots. **a**, Schematic of the optically detected NMR set-up, showing a mini-coil wound around a sample supplying an in-plane oscillating magnetic field B_{rf} . Optical excitation is along the growth axis of the dot and the external field, B_z . **b**, Rabi oscillations of ⁶⁹Ga spins in a GaAs/AlGaAs QD measured for $B_{rf} = 0.6, 1.2$ and 1.8 mT via the variation of the exciton Zeeman splitting as a function of the radiofrequency (rf) pulse duration ($B_z = 3.55$ T). Lines show fitting, taking into account inhomogeneities of the nuclear Zeeman splitting still present in strain-free GaAs QDs. **c**, Optically detected NMR spectra of strained self-assembled InP/GaInP quantum dots measured at $B_z \approx 5.3$ T using the ‘inverse’ method (see text)¹⁹ with σ^+ (red curves) and σ^- (blue curves) optical pumping. For spin-1/2 ³¹P unaffected by strain, a saturation NMR spectrum (with single-frequency excitation) is shown. The sharp single peaks correspond to $-1/2 \leftrightarrow +1/2$ central transitions, weakly affected by strain with amplitudes proportional to isotope concentrations: significant substitution of indium by gallium in InP quantum dots is evidenced in **c**. $\pm 3/2 \leftrightarrow \pm 1/2$ transitions least affected by strain (for $|I_z| > 1/2$) give rise to secondary peaks (marked by vertical arrows). Inset, high-resolution ‘inverse’ optically detected NMR spectra of central transitions measured in InGaAs QDs at $B_z \approx 5.3$ T. Arsenic-75 nuclei show greater sensitivity to strain compared with ⁷¹Ga and ¹¹⁵In, resulting in a broader NMR line. Figure reproduced from: **b**, ref. 17, © 2011 NPG; **c,d**, ref. 19, © 2012 NPG.

have a time dependence given by $\exp[-(t/T^2)^{2.3}]$ (refs 78,106). The resulting exponent of 2.3 as opposed to 4 in GaAs (refs 78,106) is a result of the detailed envelope wavefunctions associated with each system and is therefore not a universal exponent. A second example is recurrences in the electron spin-echo signal as seen in Fig. 5b. In GaAs such recurrences are a result of commensurate evolution of the nuclear spins of different species. A similar phenomenon is also seen in nitrogen–vacancy centres in diamond owing to the ^{13}C nuclear spins. But unlike the GaAs case where multiple species are required in order to see recurrences, in diamond, because the dominant interaction between the central spin and the nuclear spins is dipolar, a single nuclear spin species is sufficient.

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Competing financial interests

The authors declare no competing financial interests.